

Basic Rules for Derivatives

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|-------------------------------------|---|
| 1. $[f(x) + g(x)]' = f'(x) + g'(x)$ | 4. $[f(x)g(x)]' = f'(x)g(x) + f(x)g'(x)$ |
| 2. $[f(x) - g(x)]' = f'(x) - g'(x)$ | 5. $\left[\frac{f(x)}{g(x)}\right]' = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$ |
| 3. $[cf(x)]' = cf'(x)$ | 6. $[f(g(x))]' = f'(g(x))g'(x)$ |

Basic Derivatives

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|--|---|
| 1. $(c)' = 0$ | 12. $(\sec x)' = \sec x \tan x$ |
| 2. $(x)' = 1$ | 13. $(\csc x)' = -\csc x \cot x$ |
| 3. $(x^r)' = rx^{r-1}$, for any real number r | 14. $(\cot x)' = -\csc^2 x$ |
| 4. $(e^x)' = e^x$ | 15. $(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$ |
| 5. $(a^x)' = a^x \ln a$ | 16. $(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$ |
| 6. $(\ln x)' = \frac{1}{x}$ | 17. $(\arctan x)' = \frac{1}{1+x^2}$ |
| 7. $(\ln x)' = \frac{1}{x}$ | 18. $(\operatorname{arcsec} x)' = \frac{1}{ x \sqrt{x^2-1}}$ |
| 8. $(\log_a x)' = \frac{1}{\ln a} \frac{1}{x}$ | 19. $(\operatorname{arccsc} x)' = -\frac{1}{ x \sqrt{x^2-1}}$ |
| 9. $(\sin x)' = \cos x$ | 20. $(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$ |
| 10. $(\cos x)' = -\sin x$ | |
| 11. $(\tan x)' = \sec^2 x$ | |

Basic Rules for Indefinite Integrals

$$1. \int [f(x) + g(x)] dx = \int f(x) dx + \int g(x) dx$$

$$2. \int [f(x) - g(x)] dx = \int f(x) dx - \int g(x) dx$$

$$3. \int cf(x) dx = c \int f(x) dx$$

Basic Indefinite Integrals

$$1. \int 1 dx = x + C$$

$$2. \int x^n dx = \frac{x^{n+1}}{n+1} + C \quad \text{when } n \neq -1$$

$$3. \int \frac{1}{x} dx = \ln|x| + C$$

$$4. \int e^x dx = e^x + C$$

$$5. \int a^x dx = \frac{a^x}{\ln a} + C$$

$$6. \int \sin x dx = -\cos x + C$$

$$7. \int \cos x dx = \sin x + C$$

$$8. \int \sec^2 x dx = \tan x + C$$

$$9. \int \sec x \tan x dx = \sec x + C$$

$$10. \int \csc^2 x dx = -\cot x + C$$

$$11. \int \csc x \cot x dx = -\csc x + C$$

$$12. \int \frac{1}{\sqrt{1-x^2}} dx = \arcsin x + C$$

$$13. \int \frac{1}{1+x^2} dx = \arctan x + C$$

$$14. \int \frac{1}{|x|\sqrt{x^2-1}} dx = \operatorname{arcsec} x + C$$

Techniques of Integration

1. Substitution
2. Integration by Parts
3. Partial Fractions