

Today

Day 10

I last time

II Relative Motion

III Addition of velocities

I • Quiz on projectile

motion - more varied than previous quizzes.

- Independence of x and y motions

- x motion is const. speed

- y motion is const. accel.

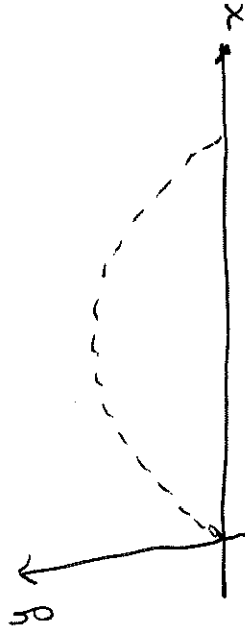
• Studied Uniform circular motion

Uniform = constant speed, but velocity is not constant, it is always tangent to the circle. Acceleration acts to change the direction of the velocity. It is always towards the center of the circle with magnitude

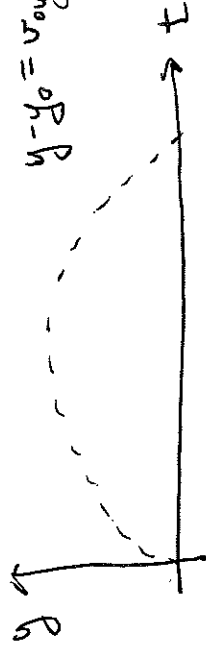
$$a = v^2/r$$

II We've been studying projectile

motion and have found



But we also found in 1D const. accel



$$y - y_0 = v_{0yt} - \frac{1}{2}gt^2$$

The reason of course, is that

$$x = x_0 + v_{0x}t$$

i.e. $x - x_0 \propto v_{0x}t$, so they are proportional to

behave exactly like one another here.

But, these notions can be seen as similar for another reason too



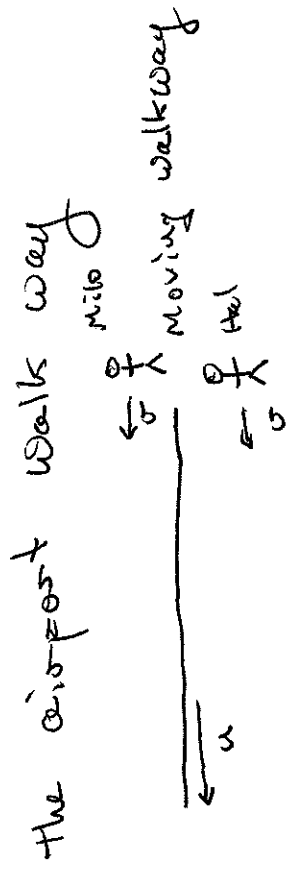
You cannot! I still find it completely remarkable that our solar system is moving at

230 km/s (= 143 mi/s = 514,000 mph) around the galactic center.

Galileo realized that all we can pin down is the relative motion of two objects: a clear example is

From the perspective of ^{P2/4} the moving observer, this is just 1D const. accel. motion in the y-direction

This insight led Galileo to the question: How can you tell if something is in motion? His surprising and profound answer was that



Both u and v are specified with respect to the ground.

A useful convention:

$$v_{AB} = \text{velocity of A w.r.t. B}$$

What is Milo's speed with respect to the ground?

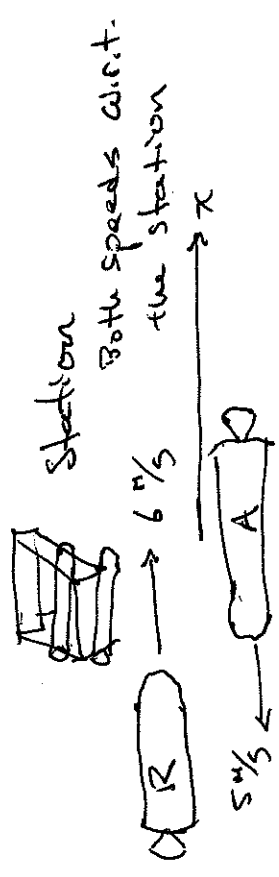
$$v_{MG} = v_{MW} + v_{WG}$$

$$= v + u$$

In general Galileo posited

$$v_{AC} = v_{AB} + v_{BC}$$

This says that whenever you know



What is v_{RA} (Russians w.r.t. Americans)?

$$v_{RA} = v_{RS} + v_{SA}$$

Space Station w.r.t. Americans

$$= v_{RS} - v_{AS}$$

Americans w.r.t. Station

$$= 6 \text{ m/s} - (-5 \text{ m/s}) = 11 \text{ m/s}$$

Let
 $M = \text{Milo}$, $H = \text{Hel}$
 $G = \text{ground}$
 $W = \text{walkway}$

Then

$$v_{HG} = v$$

$$v_{WG} = u$$

$$v_{MW} = v$$

the speed of two objects with respect to one common frame, frame B in this formula, you can figure out their speeds with respect to one another.

Ex: Two space shuttles, one Russian and one American are moving as shown with respect to a space station

What about v_{AR} ? Well,

$$v_{AR} = v_{AS} + v_{SR} = v_{AS} - v_{RS}$$

$$= -5 \text{ m/s} - (6 \text{ m/s}) = -11 \text{ m/s}$$

This confirms that

$$v_{AR} = -v_{RA} \quad \checkmark$$

Notice that the signs (as always) are determined by my choice of coordinates.