

Quantum Guest Lectures

Feb 11th 2019
P/2

I. Why linear Algebra?

II. Inner product

III. Hilbert Space

IV. Revised Inner
Product

Wave function $|\alpha\rangle$ gets rep'd by a
vector

$$|\alpha\rangle \rightarrow a = \begin{pmatrix} a_1 \\ a_2 \\ \vdots \\ a_n \end{pmatrix}$$

In the Dirac notation we have $|\beta\rangle = T|\alpha\rangle$
and it gets rep'd by

$$\vec{b} = T \vec{a} = \begin{pmatrix} t_{11} & t_{12} & \dots \\ t_{21} & & \\ \vdots & & \end{pmatrix} \vec{a}$$

To complete our definition of a Hilbert
space, we include a notion of an inner
product,

$$\langle \alpha | \beta \rangle = a_1^* b_1 + a_2^* b_2 + \dots + a_n^* b_n$$

What is the set of functions that
we are interested in? P2/2

We are interested in all the
square integrable functions on
a specified range.

Hilbert space, this is a space
of functions that forms a vector space.

Inner products: α

$$\langle \alpha | \beta \rangle = \sum_{n=1}^{\infty} a_n^* b_n$$

$$\langle f | g \rangle = \int_a^b f^*(x) g(x) dx$$

Note that

$$\langle g | f \rangle = \langle f | g \rangle^*$$

A set of functions is orthonormal
if they are orthogonal one to another
and each is normalized.