Show all appropriate work.

- 1. (a) Give four different sample spaces to describe three tosses of a coin.
  - (b) For each of your sample spaces in part (a), give the event corresponding to the statement "at most one tails is obtained," if possible.
  - (c) Is it possible to find an event corresponding to the above statement in every possible sample space for the tossing of three coins? Explain.
- 2. Three people are asked on a news show before an election whether they prefer candidate A or B or have no preference. Give two sample spaces for the possible answers.



- 3. Considering the given Venn diagram identify by numbers the following sets:
  - (a)  $(A \cup B) \cap C$ .
  - (b)  $\bar{A} \cap (\bar{B} \cap C)$ .
  - (c)  $A (B \cap C)$ .
- 4. Using the same Venn diagram, show that in general:
  - (a)  $A \cap (B \cup C) \neq (A \cap B) \cup C$ , but
  - (b)  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C),$
  - (c)  $(A \cap B) \cup C = (A \cup C) \cap (B \cup C).$
- 5. Show that  $A \subset B$  if and only if  $A \cap B = A$ .